## Group Work on Graphs CS 24, Dr. Ostheimer

Let G = (U, E) be a simple, undirected graph. G is *april-like* if there exist  $U_1, U_2 \subseteq U$  such that

- $U_1 \cup U_2 = U$ ,
- $U_1$  and  $U_2$  are disjoint, and
- for all  $\{u, v\} \in E$  either  $u \in U_1$  and  $v \in U_2$  or  $v \in U_1$  and  $u \in U_2$ .

For all of this group work, assume that by graph we mean simple, undirected graph.

- (1) For each of the questions below, draw a picture of a graph that meets the stated criteria, or state that no such graph exists
  - (a) a complete graph  $K_n$  which is also april-like
  - (b) a complete graph  $K_n$  which is not april-like

  - (d) a graph with degree sequence 3, 3, 3, 3, 3, 3, 3 that is not april-like
  - (e) a graph with degree sequence 0, 1, 1, 1, 2, 2, 3 that is april-like
  - (f) a graph with degree sequence 0, 1, 1, 1, 2, 2, 3 that is not april-like

- (2) Are the following statements true or false? Provide counterexamples for those that are false.
  - (a) If G and H have the same degree sequence, then they have the same number of vertices and edges.
  - (b) If G and H have the same number of vertices and edges, then they have the same degree sequence.
  - (c) If G and H are graphs with the same degree sequence, and if G is april-like, then so is H.